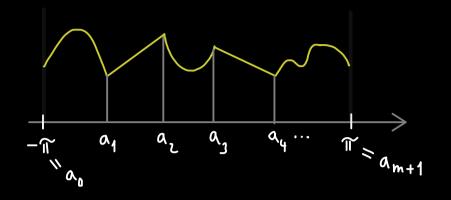


 $\implies \| \mathbf{S} \|_{\mathbf{L}^{2}} \leq \| \mathbf{S} \|_{\infty}$

Theorem: $f: \mathbb{R} \longrightarrow \mathbb{C}$ 2π -periodic <u>continuous</u> function.



Assume there are finitely many points $(a_1, a_2, ..., a_m)$ inside the interval $[-\pi, \pi]$ such that:

$$\frac{f}{\left[a_{j}, a_{j+1}\right]} \in \mathbb{C}^{1} \quad \text{for all} \quad j \in \left\{0, 1, \dots, m\right\}$$

 $\underline{\text{Then:}} \quad \left\| f - \mathcal{F}_{n}(f) \right\|_{\infty} \xrightarrow{h \to \infty} 0 \qquad \qquad \mathcal{F}_{n}(f) = \sum_{k=-n}^{n} e_{k} \langle e_{k}, f \rangle \\ e_{k} : x \mapsto e^{ikx} \\ \langle f, g \rangle = \frac{1}{2\pi} \int_{-\pi}^{\pi} f(x) \cdot g(x) \, dx \end{pmatrix}$