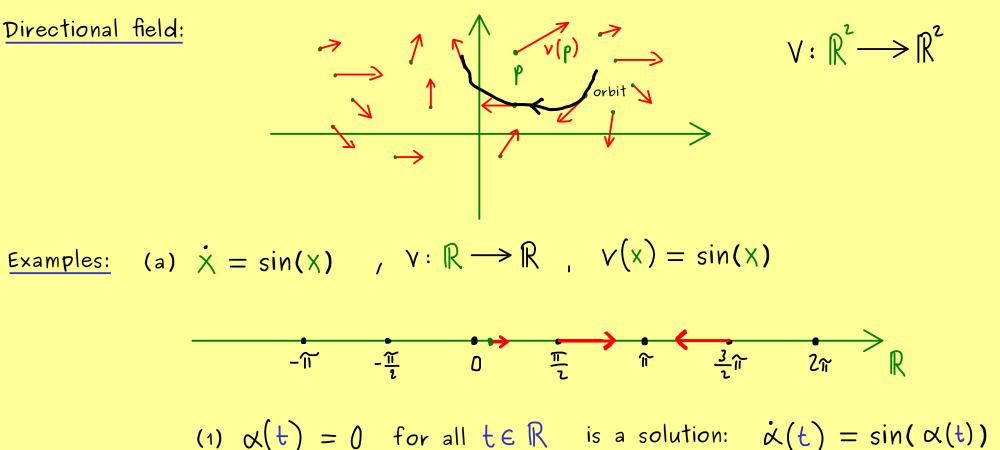
ON STEADY

The Bright Side of Mathematics



Ordinary Differential Equations - Part 3 $ODE: \dot{x} = w(t, x)$ (explicit, of first order) **Example:** (a) $\dot{x} = \lambda \cdot x$ \longrightarrow autonomous (b) $\dot{x} = t$ \longrightarrow not autonomous (c) $(\dot{x}_{1}) = (x_{1}) \longrightarrow$ autonomous $(\dot{x}_{1}) = (x_{1}) \longrightarrow$ autonomous

<u>Definition:</u> autonomous system: $\dot{X} = V(X)$ with $V: U \longrightarrow \mathbb{R}^n$ often: $V = \mathbb{R}^n$ U open $V = \mathbb{R}^n$ V continuous



$$= 0 \qquad = 0 \qquad = 0$$

(2)
$$\alpha(t) = \hat{1}$$
 for all $t \in \mathbb{R}$ is a solution.

(3) A solution with
$$\alpha(0) = \frac{\pi}{2}$$
 is monotonically increasing with $\lim_{t \to \infty} \alpha(t) = \pi$.

(b)
$$\begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} -x_1 \\ x_1 \end{pmatrix}$$
, $V: \mathbb{R}^2 \to \mathbb{R}^2$, $(x_1, x_2) \mapsto \begin{pmatrix} -x_1 \\ x_1 \end{pmatrix}$

