



 $\tilde{c}$  .  $\tilde{c}$  (1) > 0  $\tilde{c}$ 

Then f is continuous, 
$$\gamma := 0$$
, and  $f(a) \leq 0$ ,  $f(b) \geq 0$ .  
Check  $\tilde{f}(c)$ :  
Repeat If  $\tilde{f}(c) > 0$ :  $b_1 := c$ ,  $a_1 := a$   
If  $\tilde{f}(c) \leq 0$ :  $a_1 := c$ ,  $b_1 := b$ 

Wet get two <u>Cauchy</u> sequences  $(a_n)_{n \in \mathbb{N}}$ ,  $(b_n)_{n \in \mathbb{N}}$  and  $b_n - a_n \xrightarrow{h \to \infty} O$  $\implies \widetilde{X} := \lim_{n \to \infty} a_n = \lim_{n \to \infty} b_n \in [a, b]$ We know:  $\begin{array}{ccc}
\lim_{n \to \infty} \tilde{f}(a_n) \leq 0 \\
\lim_{n \to \infty} \tilde{f}(b_n) \geq 0
\end{array} \implies \begin{array}{ccc}
\tilde{f}\left(\lim_{n \to \infty} a_n\right) \leq 0 \\
\tilde{f}\left(\lim_{n \to \infty} b_n\right) \geq 0
\end{array} \implies \begin{array}{ccc}
\tilde{f}(\tilde{\chi}) \leq 0 \\
\tilde{f}(\tilde{\chi}) \geq 0
\end{array}$ 

 $\Box$ 



