ON STEADY



Unbounded Operators - Part 1



Motivation: • partial differential equations

• quantum mechanics: one needs operators X, P with  $XP - PX = i \cdot I$ 

<u>Definition</u>: Let  $(X, \|\cdot\|_{X}), (Y, \|\cdot\|_{Y})$  be normed spaces (same field  $F \in \{R, C\}$ ) and  $\mathbb{J} \subseteq X$  subspace.

A linear map  $T: \mathbb{J} \longrightarrow Y$  is called an <u>operator</u>.

Other notations:  $T: X \supseteq \mathbb{D} \longrightarrow Y$   $T: X \longrightarrow Y$  with domain  $\mathbb{D}$   $(T, \mathbb{D})$  or T with  $\mathbb{D}(T) = \mathbb{D}$ Moreover: T is called <u>densely defined</u> if  $\overline{\mathbb{D}}^{\|\cdot\|_X} = X$ .

